

Name :
Reg. No:

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APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY
07 THRISSUR CLUSTER

FIRST SEMESTER M.TECH. DEGREE EXAMINATION MARCH 2021

Civil Engineering
Structural Engineering

07 MA 6005 MATHEMATICAL METHODS IN STRUCTURAL
ENGINEERING

Time:3 hours

Max. Marks: 60

Answer all six questions. Part 'a' of each question is compulsory.

Answer either part 'b' or part 'c' of each question

Q.no. Module 1 Marks

1a Find the Extremals of the functional $\int_{x_1}^{x_2} (x + y')y' dx$ 4

Answer b or c

b Find the Extremals of $\int_{\frac{1}{10}}^1 y'(1 + x^2 y') dx$, if $y(\frac{1}{10}) = 19$, $y(1)=1$ 5

c Find the plane curve of fixed perimeter and Maximum area. 5

Q.no. Module 2 Marks

2a Explain the Principle of virtual work. 4

Answer b or c

b A Cantilever AB of length L Suppose a concentrated load of P at the free end. Determine the deflection and slope at the free end using energy principles Assume uniform flexural rigidity. 5

c Discuss the concept of strain energy and complementary strain energy. 5

Q.no. **Module 3** **Marks**

3a Examine whether the set $A = \{(x,y,z)/2x-y+3z=0\}$ is a subspace of R^3 . **4**

Answer b or c

b Reduce the Matrix $A = \begin{bmatrix} 1 & 3 & 1 \\ 2 & 6 & 4 \\ 1 & 3 & 2 \end{bmatrix}$ to echelon form and every solution to $AX=0$ **5**

c Find the Linear Transformation $T: R^2 \rightarrow R^2$ such that $T(1,3)=(5,-4)$, $T(-1,1)=(-1,0)$. Also find that $T(2,2)$ **5**

Q.no. **Module 4** **Marks**

4a If B has Eigen value 1,2,3 and C has an Eigen value 4,5,6 and D has an Eigen value 7,8,9 what are the Eigen values of the 6 by 6 matrix $A = \begin{bmatrix} B & C \\ 0 & D \end{bmatrix}$ **4**

Answer b or c

b Diagonalize the Matrix $A = \begin{bmatrix} 7 & -1 & 3 \\ 6 & 1 & 4 \\ 2 & 4 & 8 \end{bmatrix}$ and hence find A^3 **5**

c Find the orthonormal Basis of R^3 from the given Basis $B = \{(1,1,1), (0,1,1), (0,0,1)\}$ **5**

Q.no. **Module 5** **Marks**

5a Find the solution of the PDE $u_x + u_y = 0$ using method of separation of variables **5**

Answer b or c

b Classify the Following PDE and reduce to the canonical form $4u_{xx} + 5u_{yy} + u_{xy} + u_x + u_y = 2$ **7**

- c** A tightly stretched string of length 10cms fastened at both ends is displaced from its position of equilibrium by imparting to each of its points an initial velocity given by
- $$f(x)=\begin{cases} x & \text{if } 0 \leq x \leq 5 \\ 10 - x & \text{if } 5 \leq x \leq 10 \end{cases}$$
- x being the t from one end. Determine the Displacement at any subsequent time. **7**

Q.no.	Module 6	Marks
6a	Solve the two dimensional laplace equation By the method of separation of variables	5
Answer b or c		
b	Define Neuman Problem for Rectangle for solve it.	7
c	Describe Interior Dirchelet's Problem for circle and hence solve it.	7