

06ME6013

Reg. Number.....

Name.....

**A P J ABDUL KALAM TECHNOLOGICAL UNIVERSITY**  
**M.TECH DEGREE EXAMINATION, DECEMBER 2020**  
**FIRST SEMESTER**

**Energy Management**

**Numerical Methods in Heat Transfer**

Time : 3 Hours

Max. Marks: 60

**PART A**

*Answer All Questions*

1. List out 2 methods for prediction of heat transfer and fluid flow processes.
2. What is the difference between a nonlinear and a quasilinear partial differential equation?
3. What is the condition for diagonal dominance of a  $n \times n$  matrix?
4. Sketch the computational molecule for an explicit (1-D transient) scheme.

**4 x 5 marks = 20 marks**

**PART B**

5. With reference to a heated wall explain the numerical approach to problem solving.

**OR**

6. List out any 5 advantages of theoretical calculation in predicting heat transfer problems.

7. Classify the following partial differential equations:

(a)  $\frac{\partial^2 u}{\partial x^2} = \frac{1}{\alpha} \frac{\partial u}{\partial t}$

(b)  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$

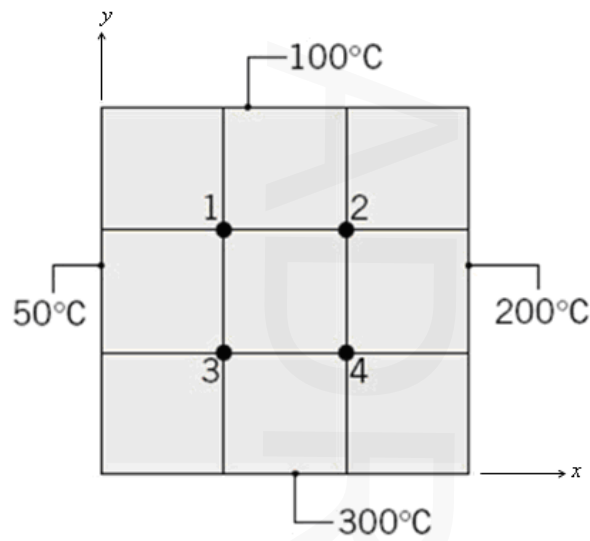
(c)  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + S = 0$

(d)  $\frac{\partial^2 u}{\partial x^2} = \frac{1}{C^2} \frac{\partial^2 u}{\partial t^2}$

**OR**

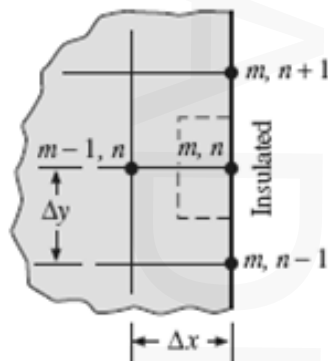
8. Obtain the first order forward difference expression for the  $x$  and  $y$  derivatives at the grid point  $(i,j)$ .

9. Solve the two-dimensional steady state conduction heat equation, over the square mesh of side 3 units, with the boundary conditions as given in the following figure.



OR

10. With respect to the following figure obtain nodal equation for equal increments in  $x$  and  $y$  corresponding to the node  $(m, n)$ .



11. Explain Crank-Nicolson method for solving one dimensional transient heat transfer problems.

OR

12. Use explicit method to solve for temperature distribution at 0.3 sec of a thin rod of 10 cm length using  $\Delta x = 2$  cm. and  $\Delta t = 0.1$  sec. At time  $t = 0$ , the temperature of the rod is zero and the boundary conditions are fixed at  $T(0) = 100^\circ C$  and  $T(10) = 50^\circ C$ . The material of the rod is aluminium with  $\alpha = 0.835 \text{ cm}^2/\text{sec}$ .

**4 x 10 marks = 40 marks**