

Reg No.: _____

Name: _____

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

Fifth Semester B.Tech Degree Examination (Regular and Supplementary), December 2020

Course Code: EE307**Course Name: SIGNALS AND SYSTEMS**

Max. Marks: 100

Duration: 3 Hours

PART A*Answer all questions, each carries 5 marks.*

Marks

- 1 Suppose $x(t) = \frac{dr(t)}{dt}$, where $r(t)$ denotes unit ramp signal. Plot the following signal $x[t + 4]x[-t + 4]$. (5)
- 2 Comment on the stability of the system with impulse response given by $h(t) = (2 + e^{-3t})u(t)$, where $u(t)$ is unit step signal. (5)
- 3 State the necessary conditions for the existence of Fourier Transform. Find the FT of $x(t) = te^{at}u(t)$. (5)
- 4 Explain the process of signal reconstruction of a sampled signal. Derive the transfer function of zero order hold? (5)
- 5 Determine the z transform of $x[n] = a^n u[n] - b^n u[-n-1]$ and find the ROC if (i) $a > b$ and (ii) $a < b$. (5)
- 6 Explain briefly the mapping of s-plane to z-plane? Show the mapping of stability regions in s-plane and z-plane. (5)
- 7 Find the Fourier series coefficients of the discrete signal $x[n] = \cos\left(\frac{\pi}{4}n\right)$? (5)
- 8 Write any five properties of nonlinear systems. (5)

PART B*Answer any two full questions, each carries 10 marks.*

- 9 Comment on the linearity, causality, time-invariance and memory of a system which finds the odd component of a given signal $x(t)$, that is, $y(t) = \text{odd}(x(t))$. (10)
- 10 a) Consider an LTI system with impulse response $h(t) = u(t + 3)$. Find the output $y(t)$, for an input $x(t) = e^{-3t}u(t)$. (5)
- b) Find the fundamental period and frequency of the signal $x(t) = 6\sin 24\pi t + 8 \sin 36\pi t$. (5)

- 11 Find the zero state response for a system with transfer function (10)

$$H(s) = \frac{s+2}{s^2+4s+3} \text{ if the input is } e^{-t}u(t).$$

PART C

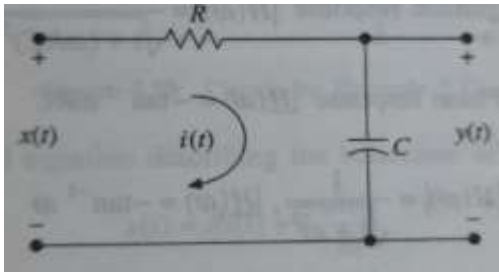
Answer any two full questions, each carries 10 marks.

- 12 Find the complex exponential Fourier series representation of the following (10)
signal. Also plot the magnitude spectrum.

$$x(t) = 4\cos 2\omega_0 t$$

Here ω_0 is the fundamental frequency in rad/sec.

- 13 Find the frequency response of the RC circuit shown below. Plot the magnitude (10)
and phase response for $RC=1$?



- 14 a) Determine the step response of a system with impulse response given by (5)
 $h[n] = a^n u[n]$.
b) Consider the analog signal $x_a(t) = 2\cos 2000\pi t + 5\sin 4000\pi t + 12\cos 12000\pi t$. (5)
Determine the Nyquist sampling rate.

PART D

Answer any two full questions, each carries 10 marks.

- 15 Solve difference equation using z-transform (10)

$$y[n] + 2y[n - 1] = x[n]$$

with $x[n] = \left(\frac{1}{3}\right)^n u[n]$, and the initial condition $y[-1] = 1$?

- 16 a) Find the inverse z-transform of (5)

$$X(z) = \frac{3z^{-1}}{(1 - z^{-1})(1 - 2z^{-1})}$$

if ROC is i) $|z| > 2$, ii) $|z| < 1$, iii) $1 < |z| < 2$

- b) Write a short note on random signals and random processes. (5)
17 a) Determine the expression for magnitude and phase response of the following (10)
system $y[n] = x[n] - 2x[n - 1] + x[n - 2]$.
