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# APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

# SIXTH SEMESTER B.TECH DEGREE EXAMINATION(S), DECEMBER 2019

#### Course Code: EE304

## **Course Name: ADVANCED CONTROL THEORY**

Max. Marks: 100

**Duration: 3 Hours** 

(5)

(5)

#### PART A

## Answer all questions, each carries 5 marks. Marks

- 1 Obtain the transfer function of a lead compensator with the help of an electrical (5) network.
- 2 Derive the transfer function of a PID Controller
- 3 Derive a relation between state equation and transfer function for LTI system. (5)
- 4 Obtain the pulse transfer function for the system shown below.



- 5 With a neat diagram explain how the describing function analysis is used to (5) determine the stability of a system?
- 6 What are jump response and limit cycles in connection with nonlinear systems? (5)
- 7 Explain with neat diagram, what is phase trajectory and phase portrait? (5)
- 8 Define positive definite and positive semi definite functions according to (5) Liapunov stability criteria, with suitable examples.

#### PART B

## Answer any two full questions, each carries 10 marks.

- 9 a) Draw the bode-plot of lag compensator and obtain an expression for maximum (6) phase lag and corresponding frequency.
- b) Explain turning of PID controller using Ziegler-Nichols tuning method. (4)
- 10 Explain the procedure for design of a lag Compensator using Bode Plot with (10) suitable example
- 11 Consider a unity feedback system with open loop transfer function (10)

$$G(s) = \frac{k}{s(s+8)}$$

Design a lead compensator to meet the following specification:

- 1. Percentage peak overshoot is 9.5%
- 2. Natural frequency of oscillations 12 rad/sec
- 3. Velocity error constant  $\geq 10$

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## PART C

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## Answer any two full questions, each carries 10 marks.

A system is described by  $\dot{x}(t) = \begin{bmatrix} 0 & 1 \\ -4 & -4 \end{bmatrix} x(t)$ 12 (5) a)

Determine state transition matrix for the system.

- b) Define controllability. Explain with a suitable example, how can we check the (5) controllability of a system?
- 13 Derive the state model of the following transfer function in, (10)
  - (i) Controllable canonical form
  - (ii) Diagonal canonical form

$$\frac{y(s)}{u(s)} = \frac{5(s+2)}{s(s+1)(s+3)}$$

Examine the stability of the system with the following characteristic equation 14 (10)using Jury's stability test.

$$z^4 - 1.2z^3 + 0.07z^2 + 0.3z - 0.08 = 0$$

# PART D

## Answer any two full questions, each carries 10 marks.

15 Identify the following non linearity and derive a describing function for the (10)same



16 Consider the following non linear differential equation.

$$\ddot{y} - \left(0.1 - \frac{10}{3}\dot{y}^2\right)\dot{y} + y + y^2 = 0$$

Find all singular points of the system, classify them and sketch the phase portrait in the neighbourhood of singular points.

- 17 a) Discuss any three non linearities present in nature.
  - b) Investigate the stability of the following non-linear system using Liapunov (4)direct method

$$\dot{x}_1 = x_2$$
  
 $\dot{x}_2 = -x_1 - x_1^2 x_2.$ 

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(10)

(6)